# 11.4 Videos Guide

#### 11.4a

• The Comparison Test:

Suppose that  $\sum a_n$  and  $\sum b_n$  are series with positive terms.

- (i) If  $\sum b_n$  is convergent and  $a_n \leq b_n$  for all n, then  $\sum a_n$  is also convergent.
- (ii) If  $\sum b_n$  is divergent and  $b_n \le a_n$  for all n, then  $\sum a_n$  is also divergent.

#### Exercise:

• Determine whether the series converges or diverges.

$$\sum_{n=2}^{\infty} \frac{1}{\sqrt{n-1}}$$

## 11.4b

- The Limit Comparison Test: Suppose that  $\sum a_n$  and  $\sum b_n$  are series with positive terms. If  $\lim_{n \to \infty} \frac{a_n}{b_n} = c$ , where c is a positive, finite number, then either both series converge or both series diverge.
- Two special cases:

  - If lim <sup>a<sub>n</sub></sup>/<sub>b<sub>n</sub></sub> = 0 AND if ∑ b<sub>n</sub> converges, then ∑ a<sub>n</sub> also converges.
    If lim <sup>a<sub>n</sub></sup>/<sub>b<sub>n</sub></sub> = ∞ AND if ∑ b<sub>n</sub> diverges, then ∑ a<sub>n</sub> also diverges.

## Exercises:

Determine whether the series converges or diverges.

## 11.4c

• 
$$\sum_{n=3}^{\infty} \frac{n+2}{(n+1)^3}$$

#### 11.4d

- $\sum_{n=1}^{\infty} \frac{6^n}{5^{n}-1}$   $\sum_{k=1}^{\infty} \frac{k \sin^2 k}{1+k^3}$   $\sum_{n=1}^{\infty} \frac{2}{\sqrt{n+2}}$